THE UNIVERSITY



**OF HONG KONG** 

Institute of Mathematical Research Department of Mathematics

## **Optimization and Machine Learning Seminar**

## Sum-of-squares hierarchies for polynomial optimization and the Christoffel-Darboux kernel

**Mr. Lucas Slot** Centrum Wiskunde & Informatica, Amsterdam

## Abstract

We consider Lasserre's approximation hierarchies for the problem of minimizing a polynomial f over a compact semialgebraic set X in  $\mathbb{R}^n$ . When X is the unit ball or the standard simplex, we show that the hierarchies based on Schmüdgen-type positivity certificates of degree r converge to the global minimum of f at a rate in  $O(1/r^2)$ , matching recently obtained convergence rates for the hypersphere and hypercube  $[-1,1]^n$ . For our proof, we establish a connection between Lasserre's hierarchies and the Christoffel-Darboux kernel, and make use of closed form expressions for this kernel derived by Xu.

Date: March 24, 2022 (Thursday) Time: 4:00 – 5:00pm (Hong Kong Time) Venue: ZOOM: <u>https://hku.zoom.us/j/</u> Meeting ID: 940 0962 9889 Password: 286660

All are welcome