2009 – 10 Course Selection for BScII – III Major or Minor in Mathematics Dr. Yung Siu Pang Department of Mathematics HKU

Major in Mathematics (students admitted in 2006 or before)

1. Introductory Level Courses (30 credits) MATH1101 Linear Algebra I

MATH1101 MATH1102 MATH1201 MATH1202 MATH1001

Linear Algebra II Calculus I Calculus II Fundamental Concepts of Mathematics

2. Advanced Level Courses (48 credits) MATH2301 Algebra I MATH2401 Analysis I

Plus at least 36 credits of advanced level Mathematics course (MATH2XXX or MATH3XXX level)

Major in Mathematics (students admitted in 2007 or after)

1. Introductory level courses (18 credits)

MATH1001 Fundamental Concepts of MathematicsMATH1111 Linear AlgebraMATH1211 Multi-variable Calculus

2. Advanced level courses (48 credits) MATH2201 Introduction to Mathematical Analysis MATH2301 Algebra I MATH2401 Analysis I

Plusat least 18 credits from the following courses:MATH2304Introduction to Number TheoryMATH2403Functions of a Complex VariableMATH2405Differential EquationsMATH2600Discrete MathematicsMATH2601Numerical AnalysisMATH2603Probability TheoryMATH2901Operations Research IMATH2904Introduction to Optimization

Plus at least 12 credits of advanced level Mathematics courses (MATH2XXX or MATH3XXX level), subject to prerequisite requirements.

MATH2301 Algebra I

- Study of groups, rings and fields.
- Useful to MATH3302
 Algebra II, MATH3310
 Topics in Algebra and
 MATH3502 Geometric
 Topology.
- Teacher: Prof. J.H. Lu (UC Berkeley)



MATH2401 Analysis I

- Study metric topology and several important results in multi-variable differential calculus.
- Prerequisite of almost all pure mathematics courses.
- Teacher: Prof. W.S. Cheung (*Harvard*)



Major in Mathematics

Most math majors follow one of the following three main themes:

- (Pure) Mathematics (Math)
- Computational Mathematics, Logistics/ Operations Research (CMOR)
- Mathematics, Economics and Finance (MAEF)

Major in Mathematics - Math

Recommended Courses:

MATH2303 Matrix Theory and its Applications
MATH2304 Introduction to Number Theory
MATH2402 Analysis II
MATH2403 Functions of a Complex Variable
MATH3302 Algebra II
MATH3404 Functional Analysis
MATH3501 Geometry
MATH3502 Geometric Topology

MATH2001 Development of Mathematical Ideas MATH3406 Introduction to Partial Differential Equations

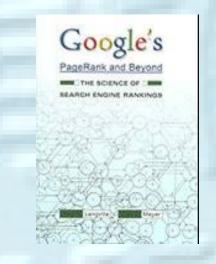
MATH2303 Matrix Theory and its Applications

- Second course in Linear Algebra
- Useful to MATH2601
 Numerical Analysis,
 MATH3602 Scientific
 Computing and Operation
 Research courses
- Related to MATH3404 Functional Analysis
- Teacher: Dr. Y.M. Chan (*Oxford*)



MATH2303 Matrix Theory and its Applications





- Matrix theory is extremely useful in the studies of applied and pure mathematics, statistics, economics, finance, engineering, etc.
- For example, it is used in image processing and search engines like Google.
- See the book, *Google's PageRank and beyond : the science of search engine rankings* by Amy N. Langville and Carl D. Meyer.

MATH1111 Linear Algebra



Larry Page

Sergey Brin

"The heart of our software is PageRank[™], a system for ranking web pages developed by our founders Larry Page and Sergey Brin at Stanford University."

MATH2402 Analysis II

- Modern treatment of calculus in several variables.
- Introduction to the concept of differential forms and manifolds ("higher dimensional surface").
- Useful to the studies of Differential and Algebraic Geometry and General Relativity, etc.
- Teacher: Prof. W.S. Cheung (Harvard)

MATH2402 Analysis II

The one – variable fundamental theorem of calculus:

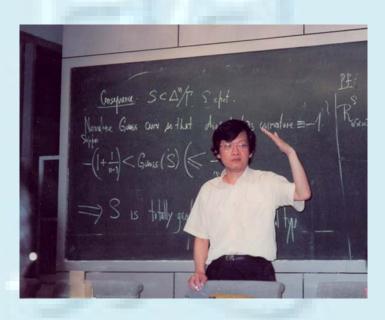
$$\int_{a}^{b} f'(x) dx = f(b) - f(a)$$

is generalized to manifold: Stokes' theorem

$$\int_{\partial c} \omega = \int_{c} d\omega$$

MATH2403 Functions of a Complex Variable

- Carry out calculus on the complex plane.
- Study of "differentiable" functions of a complex variable which have many nice and interesting properties.
- Useful to the studies of almost all branches of pure mathematics and theoretical physics such as quantum mechanics.
- Teacher: Prof. N. Mok (*Stanford*)



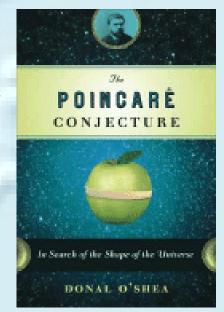
MATH3501 Geometry

- Use multi-variable calculus to study geometry of curves and surfaces in 3-space.
- Useful to the studies of Differential and Algebraic Geometry and General Relativity, etc.
- Teacher: Prof. J.H. Lu (*UC Berkeley*)



MATH3502 Geometric Topology

- Introduction to Algebraic Topology.
- Useful to the studies of Differential and Algebraic Geometry and General Relativity, etc.
- For recent important breakthrough in topology, see the book *The Poincaré conjecture: in search of the shape of the universe* by Donal O'Shea.
- This course is not offered in the academic year 2009 10.



Recommended courses:

MATH2303 Matrix Theory and Its Applications MATH2601 Numerical Analysis MATH2603 Probability Theory MATH2901 Operations Research I MATH2904 Introduction to Optimization MATH2905 Queuing Theory and Simulation MATH3602 Scientific Computing MATH3902 Operations Research II MATH3903 Network Models in Operations Research

MATH3610 Topics in Applied Discrete Mathematics MATH3910 Topics in mathematical Programming and optimization BUSI1003 Introduction to Management Information System CSIS1119 Introduction to Data Structures and Algorithms ECON0701 Introductory Econometrics STAT3301 Time-series Analysis

- Courses in Computational Mathematics and Operations Research are taught by experts in these two areas.
- For operations research: Prof. S.C.K. Chu (*Columbia*) Dr. W.K. Ching (*CUHK*) Prof. W. Zang (*Rutgers*)
- For computational mathematics: Dr. K.H. Chan (*CUHK*) Dr. G.Y. Han (*Notre Dame*)

The operations research courses mainly study different types of the constraint optimization problems.

Operations Research Group Prof. S.C.K. Chu, Prof. W. Zang, Dr. W.K. Ching (Prof. K.P. Ng)



Constrained Optimization Problem:

- Max/Min $f(x_1,...,x_n)$ under the constraints $g_i(x_1,...,x_n)=0$, i=1,...,m.
- MATH2901 Operational Research I and MATH3902 Operational Research II study this optimization problem when all these functions are linear.
- MATH2904 *Introduction to Optimization* studies the same optimization problem when some of these functions are non-linear by using multi-variable calculus.
- Numerical methods may be employed.



Constrained Optimization Problem (an example):

Customers redistribute themselves based on the perceived service performance (queuing time and traveling time) and customer loyalty.Goal: Try to predict the final customer redistribution.

Job Opportunities:

- Logistics companies
- Airport Authority Hong Kong
- Banks (data mining)
- Software companies

Major in Mathematics – MAEF

Recommended courses:

- MATH2906 Financial Calculus
- MATH2907 Numerical Methods for Financial Calculus
- BUSI1002 Introduction to Accounting
- ECON2101 Microeconomics Theory
- ECON2102 Macroeconomics Theory
- FINA1001 Introduction to Finance
- FINA2802 Investments

Major in Mathematics Minor in Economics or Finance or Risk Management!

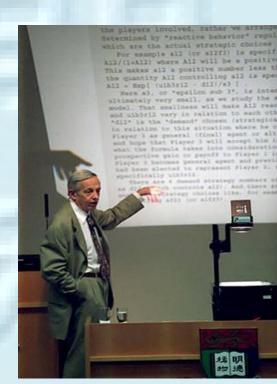


Students can prepare the level I examination of *Chartered Financial Analyst* by taking suitable courses in this category.

Major in Mathematics – MAEF

Nobel Prize (Economics) Laureates since 90's of the last century who have a math degree:

- 2007 Eric S. Maskin (PhD in applied math)
- 2007 Roger B. Myerson (PhD in applied math)
- 2005 Robert J. Aumann (BS, MS, PhD in math)
- 2004 Edward C. Prescott (BA in math, MS in operations research)
- 2003 Clive W. J. Granger (BA in math)
- 2002 Daniel Kahneman (BA in math and psychology)
- 2001 Michael Spence (BA, MA in math)
- 2000 James J. Heckman (BA in math)
- 1998 Amartya Sen (BA minor in math)
- 1997 Robert C. Merton (BS, MS in applied math)
- 1996 James A. Mirrlees (MA in math)
- 1996 William Vickrey (BS in math)
- 1994 John F. Nash Jr. (PhD in math)
- 1994 Reinhard Selten (PhD in math)
- 1992 Gary S. Becker (BA in math)



John F. Nash Jr. in HKU



Mathematics is the common language in these areas and it is easier to learn math when you are young.

Major in Mathematics – MAEF

Luo Guannan (a math major) is now doing a PhD in Economics at Northwestern University.

If you plan to do a master or PhD in economics or finance, the following courses are recommended:

MATH2401 Analysis I MATH2901/3902 OR I and II MATH2904 Introduction to Optimization MATH2911 Game Theory and Strategy MATH2906 Financial Calculus MATH2907 Numerical Methods for Financial Calculus STAT3301 Time-series Analysis STAT3316 Advanced Probability



Many investment banks employ mathematicians to do risk management or computational finance.



Dr. Lau Chi Fong (PhD in number theory) Former Head of Market Risk Management HSBC Global Markets

- Usually need a PhD in Mathematics/Physics/Computer Sciences/Statistics to do quantitative finance in investment banks.
- Develop and analyze new financial products.
- Write programs to evaluate the price of financial derivatives.
- Mathematical modeling skills.
- Computing skills, e.g., Visual Basic.

Recommended courses:

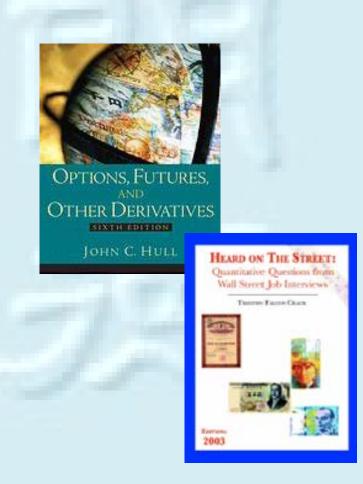
- MATH2906 Financial Calculus
- MATH2907 Numerical Methods for Financial Calculus
- MATH2603 Probability Theory
- MATH2601 Numerical Analysis
- MATH3602 Scientific Computing
- MATH3406 Introduction to PDE
- STAT3301 Time-series Analysis
- STAT3316 Advanced Probability

MATH2906 Financial Calculus

- Modeling of financial derivatives, asset pricing and market risks
- Introduction to stochastic calculus
- Provide a solid background for future study in quantitative finance.
- Prerequiste:MATH2603 Probability Theory
- Good knowledge of partial differential equations and probability theory is needed for further studies.

Suggested Readings:

- Options, futures, and other derivatives by John C. Hull
- An elementary introduction to mathematical finance by Sheldon M
- Heard on the street : quantitative questions from Wall Street job interviews by Timothy Falcon Crack.



General Mathematics Courses

- MATH0011 Numbers and Patterns in Nature and Life
- MATH2001 Development of Mathematical Ideas
- MATH2304 Introduction to Number Theory
- YSCN0002 Mathematics: A Cultural Heritage
- YSCN0034 Hidden Order in Daily Life: A Mathematics Perspective

MATH2304 Introduction to Number Theory

Dr. YK Lau (*HKU*)

Expert in modular forms and L-functions



Prof. KM Tsang (*Princeton*)

Expert in Riemann's zeta function and analytic number theory.

Student of Prof. Atle Selberg (1950 Fields-Medallist)

Prerequisites: MATH1111 and MATH1211 Co-requisite: MATH2301. Enrollment needs instructors' approval.

MATH2304 Introduction to Number Theory

Strong tradition in number theory in our department

Prof. K.M. Tsang



Prof. M.C.Liu

World expert in Goldbath' s conjecture

Fields-Medallist, Prof. Alan Baker

YSCN0034 Hidden Order in Daily Life: A Mathematical Perspective

Through exploring non-technically some mathematically rich daily life topics, this course aims to help students gain essential mathematical literacy for living in the 21st century.

Students will learn the mathematical concepts and principles of things that they encounter in the modern society, and learn how to handle and interpret numerical and other forms of mathematical data that affect their daily life. YSCN0034 Hidden Order in Daily Life: A Mathematical Perspective

Some selected topics are:

- Game Theory and Auction
- Mathematics of Voting
- Some Mathematical Principles of the Stock Markets
- Mathematics in the Courtroom
- Benford's Law and Detecting Fraud in Accounting Data

Major in Mathematics (requirement)

3. Experiential Learning Requirement (6 credits) Students (admitted in 2007 or after) must take at least one of the following forms of extraordinary – learning experience to fulfill the capstone requirement:

MATH2002 Mathematics seminar (6 credits) MATH2999 Directed studies in mathematics (6 credits) MATH3988 Mathematics Internship (6 credits) MATH3999 Mathematics project (<u>12</u> credits) Exchange programme via HKU World Wide Exchange Programme (1 semester or 1 year) (non – credit bearinig)[#]

4. Students also need to take two Science Faculty electives: One course from Block B (The Physical World) and one course from Block C (Life & Living)

Students must take an additional 6-credit advanced level mathematics course.

- This course is offered in the 2nd semester.
- This is a seminar style course intended for those year one students who have very strong interests and good ability in mathematics.
- Study some book chapters and elementary research articles and make presentations in front of the whole class.
- Active participation in all the discussions is expected. The aim of the course is to let students learn how to initiate self/independent study in mathematics.

- Prerequisites: MATH1001, MATH1111 and MATH1211 (one of MATH1111 and MATH1211 can be co-requisite).
- Enrollment needs instructors' approval.
- Quota:12.
- It will be run by Prof. K.M. Tsang, Dr. N.K. Tsing and Dr. S.P. Yung this year.

- Teaching: Meeting of the whole class for two hours each teaching week, plus individual meetings with the instructors.
- Assessment:
 - Coursework assessment (70%), based on class presentations, participation in discussions and a written report.
 - Final written examination of 2 hours (30%).

The following topics were covered last year.

- Convex geometry (Helly's theorem)
- Euler's characteristics
- Hyperbolic geometry (Basic notions)
- Isoperimetric problem
- Markov chain
- Marriage's lemma
- Mathematics in voting (Arrow' Impossibility Theorem)
- Pagerank algorithm
- Sperner's lemma
- SIR model
- Zorn's Lemma

MATH2999 Directed Studies in Mathematics

This course is designed for a student who would like to take an early experience on independent study. It provides the student with the opportunity to do a small mathematics project close to research in nature independently.

Selected topics in the past years:

- Exploration of the technical analysis of finance data
- Fibonacci sequence, the golden ratio, and patterns in plants: Phyllotaxis
- The Plateau problem
- Microarray data and diagnosis of cancer
- Positive rational solutions to some diophantine equations
- Coxeter Groups
- Riemann surfaces and / or complex manifolds
- Linear geometry in Euclidean 4-space
- Open problems in affine algebraic geometry and commutative/noncommutative algebra

MATH3988 Mathematics Internship

This course aims to offer students the opportunities to gain work experience in the industry related to their major of study. Students have to take on at least 120 hours of internship work either within the University or outside the University arranged by the School/Departments.

Available in 1st, 2nd, and the summer semester.

Assessment: Required to submit a written report and to give a presentation on their internship experience. This course will be assessed on **Pass or Fail** basis.

MATH3988 Mathematics Internship

In the past years, our students interned at various organizations: for example

- AECOM: A Fortune 500 company, serves clients in more than 100 countries and provides professional technical and management support services to a broad range of markets, including transportation, facilities, environmental and energy.
- Hong Kong Observatory
- Secondary school

Teachers in the Math Department also offered internship in the summer.

MATH3999 Mathematics Projects

The object is to provide a student with an opportunity to formulate and investigate, in depth, a problem of practical interest and/or have a foretaste of mathematical research. The work, to be done on an individual basis, is considered a highly desirable part of the training of a mathematician.

MATH3999 Mathematics Projects

Topics:

- Nonnegative matrices and their Perron roots (Dr. J.T. Chan)
- Numerical Simulation in Fluid Dynamics (Dr. K.H. Chan)
- Calculus of Variations (Professor W.S. Cheung)
- Genetic Regulatory Networks and Probabilistic Boolean Networks (Dr. W.K. Ching)
- Project Scheduling via Network Models: independent study & computer implementation (Professor S.C.K. Chu)
- Mathematical Problems in Network Coding (Dr. G.Y. Han)
- Arithmetical Functions and Dirichlet Series (Dr. Y.K. Lau)
- Introduction to Algebraic Geometry (Professor J. Lu)
- Solving Non-Linear Differential Equations (Dr. T. W. Ng)
- Dirichlet's Divisor Problem (Professor K.M. Tsang)
- Higher Rank Numerical Ranges (Dr. N.K. Tsing)
- Supersymmetric Quantum Mechanics and the Witten Index (Dr. S. Wu)

Exchange Programme (non – credit bearing)



MIT

University of California, Berkeley





University of Lund

Further Studies

Columbia University

New York University



What should I do if I want to be a minor in mathematics ?

Minor in Mathematics (requirement)

1. Introductory level courses (12 credits) MATH1111 Linear Algebra

Plus one of the following courses

MATH1211 Multi – variable Calculus MATH1805 University Mathematics B MATH1813 Mathematical Methods for Actuarial Science

Advanced level courses (24 credits)
 Any 24 credits of advanced level Mathematics courses (MATH2XXX or MATH3XXX level), subject to prerequisite requirements.

If you are interested in mathematics and would like to be a minor in mathematics, the following courses are recommended:

MATH2001 - Development of Mathematical Ideas MATH2201 - Introduction to Mathematical Analysis MATH2301 - Algebra I MATH2405 - Differential Equations MATH2600 - Discrete Mathematics MATH2601 - Numerical Analysis MATH2603 - Probability Theory MATH2901 - Operations Research I

If you would like to be a minor in math and plan to pursue a master/PhD in economics/finance, the following courses are recommended:

MATH2401 Analysis I MATH2901/3902 Operations Research I/II MATH2904 Introduction to Optimization MATH2906 Financial Calculus MATH2907 Numerical Methods for Financial Calculus STAT3301 Time-series Analysis STAT3316 Advanced Probability

If you would like to be a minor in math and plan to pursue a master/PhD in computational/mathematical finance in the future, the following courses are recommended:

MATH2906 Financial Calculus MATH2907 Numerical Methods for Financial Calculus MATH2603 Probability Theory MATH2601 Numerical Analysis MATH3602 Scientific Computing MATH3406 Introduction to PDE STAT3301 Time-series Analysis STAT3316 Advanced Probability

If you would like to be a minor in math and plan to pursue a master/PhD in computational/mathematical finance in the future, the following courses are recommended

MATH2906 Financial Calculus MATH2907 Numerical Methods for Financial Calculus MATH2603 Probability Theory MATH2601 Numerical Analysis MATH3602 Scientific Computing MATH3406 Introduction to PDE STAT3301 Time-series Analysis STAT3316 Advanced Probability Bridging Courses in Mathematics

Students with different mathematics background can major or minor in mathematics by taking suitable bridging courses and follow different paths.

For more information, please visit the following link http://hkumath.hku.hk/~wkc/advisor_major.htm Differentiate yourself from the competitions

Major in math is a good indicator:

Good in Math = Intelligent

Good in Math = Flexible

Further Enquiries: Course Selection Advisors

Year One: Dr. Y.K. Lau (<u>yklau@maths.hku.hk</u>) Dr. C.W. Wong (<u>cwwongab@hkusua.hku.hk</u>)

Year Two and Three: Dr. G. Han (<u>ghan@maths.hku.hk</u>) Dr. S.P. Yung (<u>spyung@hkucc.hku.hk</u>) (2nd sem) Prof. W. Zang (<u>wzang@maths.hku.hk</u>) (1st sem)

http://hkumath.hku.hk/web/info/math_student.html

End