



*Institute of Mathematical Research
Department of Mathematics*

GEOMETRY SEMINAR

Semi-positivity and abundance problem in Algebraic Geometry

Professor Andrey Todorov

University of California, Santa Cruz, USA

Abstract

It is a well known Theorem of Kodaira, that some power of a line bundle with a positive Chern class defines a projective embedding. In this talk we will discuss the following problems:

1. Suppose that a line bundle has a semi-positive Chern class on a projective algebraic variety. Is it true that some power of the line bundle defines a fibration of the projective manifold.
2. When can the boundary classes of the cohomologies of the Kähler cone be realized as semi-positive forms?

We will show that the second problem can be solved for CY manifold and it is related to a problem of Donaldson which states: Suppose that we fix two classes of cohomologies in the Kähler cone and realize one of the them as a imaginary part of a Kähler metric. What is the topological condition on the two classes of cohomologies that guarantees that we can find a Kähler metric in the other class of cohomolgy such that the fixed Kähler form is a harmonic form with respect to the second Kähler metric.

| | |
|---------------|--|
| Date: | March 18, 2009 (Wednesday) |
| Time: | 4:00 - 5:00pm |
| Place: | Room 517, Meng Wah Complex, HKU |

All are welcome