



*Institute of Mathematical Research  
Department of Mathematics*

## COLLOQUIUM

# $G_2$ and the Rolling Ball

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### **Abstract**

Finding concrete models for exceptional groups has been a goal in mathematics since their discovery. Here we describe a model of the smallest exceptional group,  $G_2$ , essentially due to Cartan: Locally, it gives the symmetries of one ball rolling on a fixed ball without slipping or twisting, but only when the balls have ratio of radii 1:3 or 3:1. We use the octonions to construct a similar, but more global picture of  $G_2$ : it is the symmetry group of a 'spinorial ball' rolling on a projective plane, again when the ratio of radii is 1:3 or 3:1, and we use the geometry of this system to explain this mysterious ratio.

<b>Date:</b>	<b>May 2, 2013 (Thursday)</b>
<b>Time:</b>	<b>4:00 - 5:00pm</b>
<b>Place:</b>	<b>Room 210, Run Run Shaw Bldg., HKU</b>

*All are welcome*