THE UNIVERSITY



**OF HONG KONG** 

Institute of Mathematical Research Department of Mathematics

## **Optimization and Machine Learning Seminar**

How does generalization behave under suitable model capacities in modern machine learning? From deterministic equivalence to function spaces Prof. Fanghui Liu

University of Warwick, UK

## Abstract

In this talk, I will discuss some fundamental questions in modern machine learning:

- What is a suitable model capacity of a modern machine learning model?

- How to precisely characterize the test risk under such a model capacity?

- What is the corresponding function space induced by such a model capacity?

- What are the fundamental limits of statistical/computational learning efficiency within space?

My talk will partly answer the above questions, through the lens of norm-based capacity control. By deterministic equivalence, we provide a precise characterization of how the estimator's norm concentrates and how it governs the associated test risk. Our results show the predicted learning curve admits a phase transition from under- to over-parameterization, but no double descent behavior, and reshapes scaling laws as well. I will talk about the path-norm based capacities and the induced Barron spaces to understand the fundamental limits of statistical efficiency, particularly in terms of sample complexity and dimension dependence – highlighting key statistical-computational gaps.

Date: July 30, 2025 (Wednesday) Time: 4:00 pm – 5:00 pm Venue: Room 210, Run Run Shaw Building HKU

All are welcome